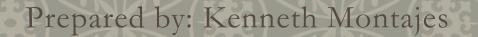
# LINES

MATH 17



# Pythagorean Theorem

In a right triangle, if a and b are the lengths of the perpendicular sides and c is the length of the hypotenuse, then



#### Undirected distance between two points

• The distance between two points  $P_1(x_1, y_1)$  and  $P_2(x_2, y_2)$  is given by

$$|\overline{P_1P_2}| = ?$$

#### Undirected distance between two points

Find the distance of the points A(-4,7) and B(1,-3)



### Midpoint Formula

• If M(x, y) is the midpoint of the line segment from  $P_1(x_1, y_1)$  to  $P_2(x_2, y_2)$ , then

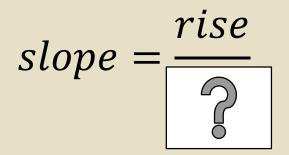




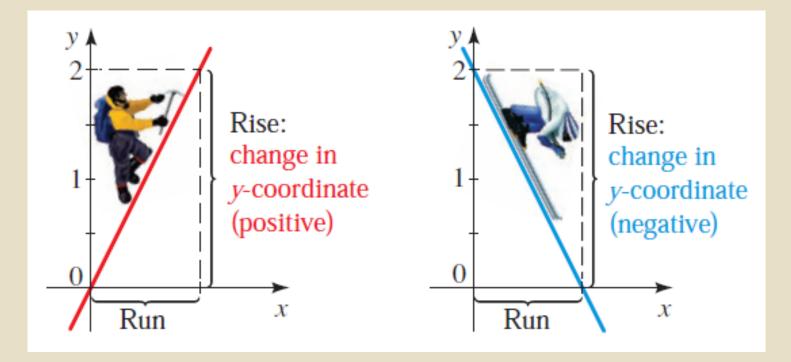
### Midpoint Formula

Find the midpoint of the points A(-4,7) and B(1,-3).

- "steepness"
- how quickly its rise (or fall)





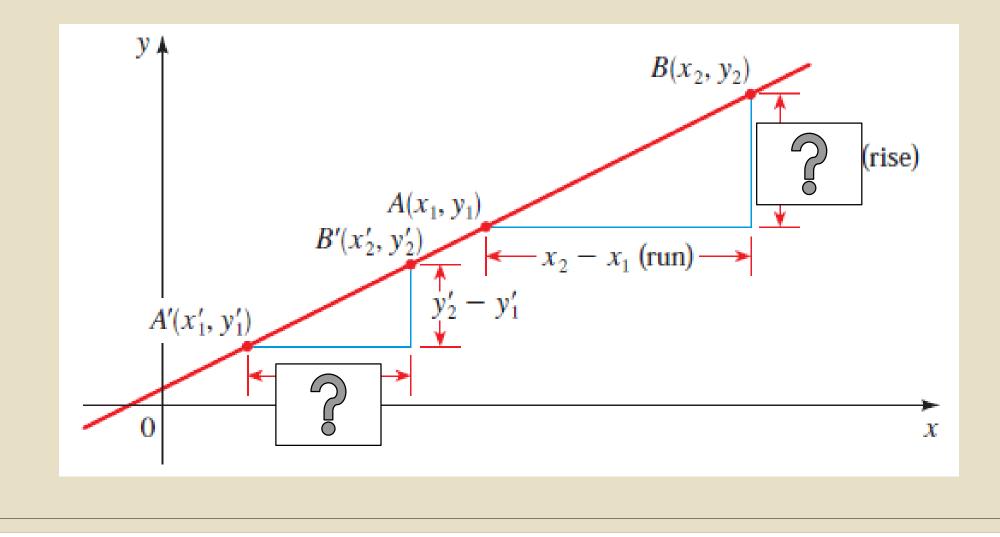


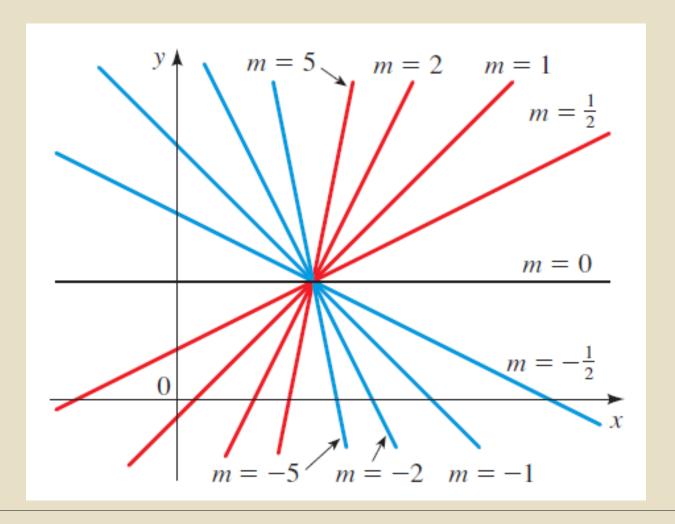
- Run: change in the *x*-coordinate
- Rise: change in the



### The **slope** *m* of a nonvertical line that passes through the points $A(x_1, y_1)$ and $B(x_2, y_2)$ is

$$m = \frac{\text{rise}}{\text{run}} = 2$$
The slope of a vertical line is

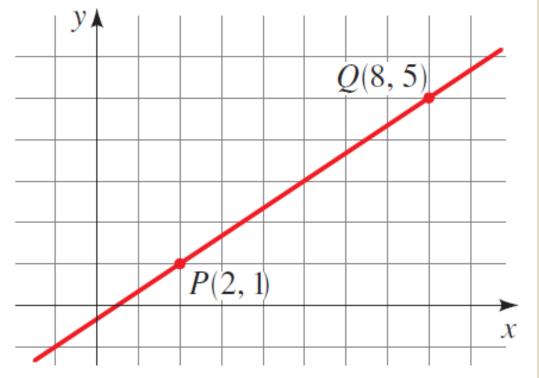


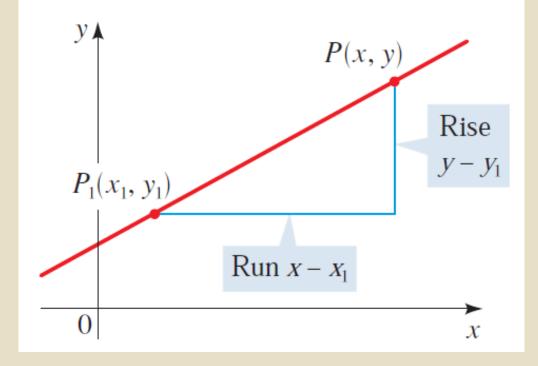


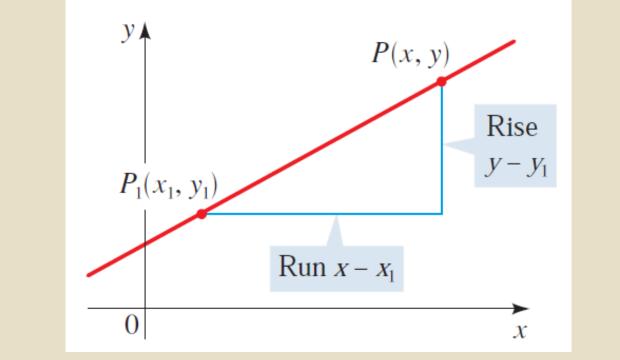
Find the slope of the lines that passes through points P(2,1) and Q(8,5).



Find the slope of the lines that passes through points P(2,1) and Q(8,5).







An equation of the line that passes through the point  $(x_1, y_1)$  and has slope *m* is

Find an equation of the line through (1, -3) with slope  $-\frac{1}{2}$ 

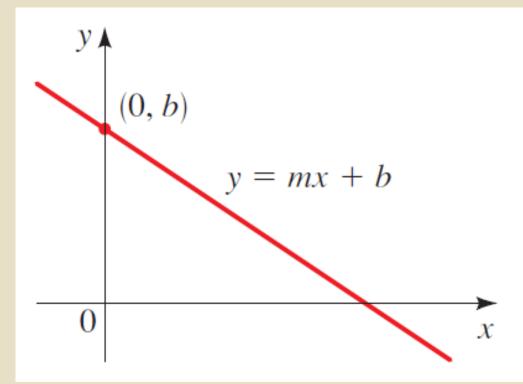


Find an equation of the line through (1, -3) with slope  $-\frac{1}{2}$ Ó 0 Run = 2Rise = -1

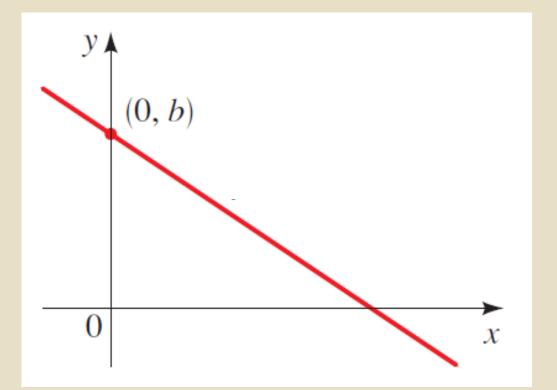
Find an equation of the line through (-1,2) and (3,-4)



# Slope-Intercept form



# Slope-Intercept form



An equation of the line that has slope *m* and *y*-intercept *b* is

# Slope-Intercept form

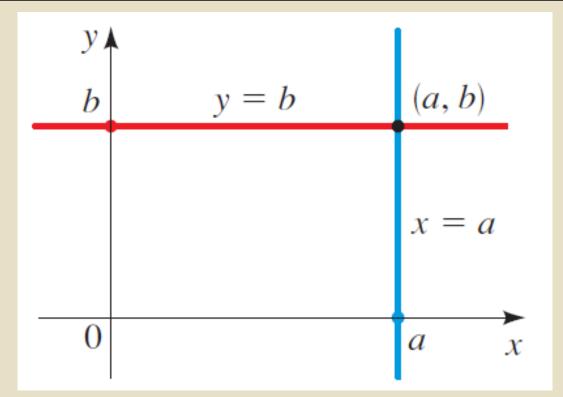
Find the equation of the line with slope 3 and y-intercept -2

#### Find the slope and y-intercept of the line 3y - 2x = 1





#### Vertical and Horizontal Lines

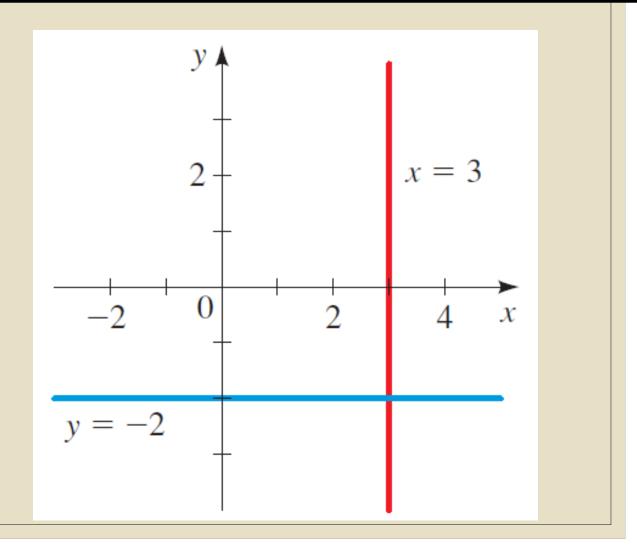


An equation of the vertical line through (a, b) is x = a. An equation of the horizontal line through (a, b) is y = b.

#### Vertical and Horizontal Lines

An equation for the vertical line through (3,5) is x = 3

An equation for the horizontal line through (8, -2) is y = -2



### General Equation of a Line

A linear equation is an equation of the form

where A, B, and C are constants and A and B are not both 0.

### General Equation of a Line

An equation

$$Ax + By + C = 0$$

with  $B \neq 0$  has slope-intercept form



and if B = 0, the equation becomes

$$Ax + C = 0$$

or

$$x = -\frac{C}{A}$$

### General Equation of a Line

Sketch the graph of the equation

$$2x - 3y - 12 = 0$$

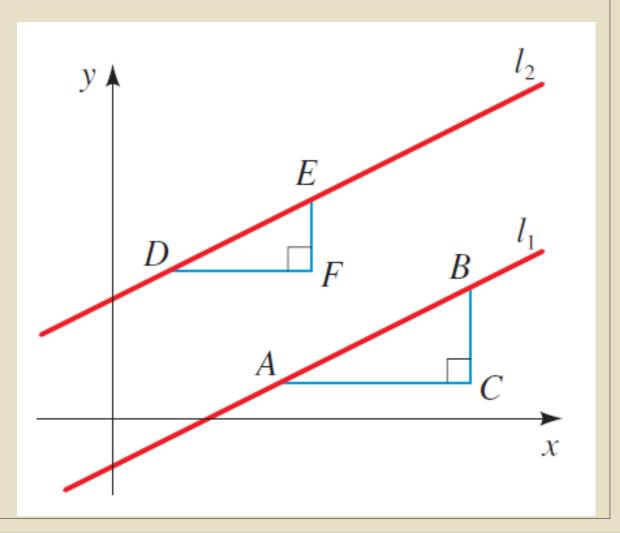
using intercepts and using the slope-intercept form

Two nonvertical lines are parallel if and only if they have the same



Proof: Let lines  $l_1$  and  $l_2$  have slopes  $m_1$  and  $m_2$ . If the lines are parallel then the right triangles *ABC* and *DEF* are similar, so

$$m_1 = \frac{d(B,C)}{d(A,C)} = \frac{d(E,F)}{d(D,F)} = m_2$$



# Find an equation of the line through the point (5,2) that is parallel to the line 4x + 6y + 5 = 0



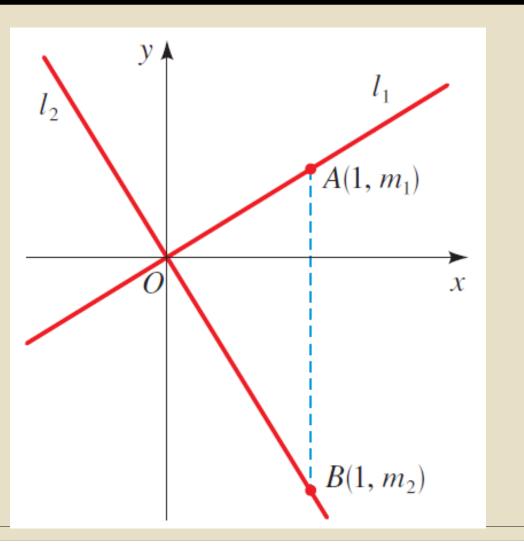
Two lines with slopes  $m_1$  and  $m_2$  are perpendicular if and only if  $m_1m_2 = -1$ , that is, their slopes are negative reciprocals:

$$m_2 = -\frac{1}{m_1}$$

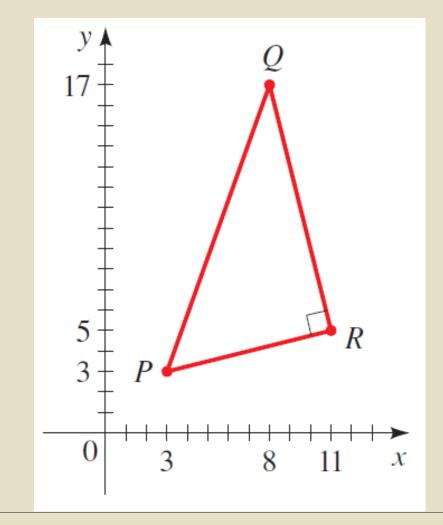
Also, a horizontal line (slope 0) is perpendicular to a vertical line (no slope).

#### Proof:

If the lines  $l_1$  and  $l_2$  have slopes  $m_1$  and  $m_2$ , then the equations are  $y = m_1 x$  and  $y = m_2 x$ .



Show that the points P(3,3), Q(8,17), and R(11,5) are the vertices of a right triangle.



Show that the points P(3,3), Q(8,17), and R(11,5) are the vertices of a right triangle.

Find an equation of the line that is perpendicular to the line 4x + 6y + 5 = 0 and passes through the origin

